Homework #1

Chapter 15

Chemical Kinetics

8. Arrhenius Equation

 $k = A e^{E_a/_{RT}}$

Therefore, k depends only on temperature. The rate of the reaction depends on all of these items (a-d).

- 14. a) $\frac{mol}{L \cdot s}$ b) $\frac{mol}{L \cdot s}$ c) $\frac{1}{s}$ d) $\frac{L}{mol \cdot s}$ e) $\frac{L^2}{mol^2 \cdot s}$
- 15. Rate has units of $\frac{mol}{L \cdot s}$ therefore, the units of the rate constant must compensate for any missing/additional units.

$$\frac{L^{1/2}}{mol^{1/2 \cdot s}}$$

18. a) General Rate Law

$Rate = k[NO]^{x}[Cl_{2}]^{y}$

Experiment	[NO] _o (M)	[Cl ₂] _o (M)	Initial Rate $\left(\frac{mol}{L \cdot min}\right)$
1	0.10	0.10	0.18
2	0.10	0.20	0.36
3	0.20	0.20	1.45

From experiments 1 and 2 ([NO]_o is kept constant) as the initial concentration of Cl_2 is doubled, the initial rate of the reaction doubles $\binom{0.36}{0.18}=2.0$; therefore, the reaction is first order with respect to Cl_2 .

From experiments 2 and 3 ($[Cl_2]_0$ is kept constant) as the initial concentration of NO is doubled, the initial rate of the reaction quadruples $\left(\frac{1.45}{0.36}=4.0\right)$; therefore, the reaction is second order with respect to NO.

$$Rate = k[NO]^{2}[Cl_{2}]$$

b)
$$Rate = k[NO]^{2}[Cl_{2}]$$
$$0.18 \frac{mol}{L \cdot min} = k(0.10 \text{ M})^{2}(0.10 \text{ M})$$
$$k = 180 \frac{L^{2}}{mol^{2} \cdot min}$$

a) General Rate Law

19.

$Rate = k[I^-$	$]^{x}[OCl^{-}]^{y}$		
Experiment	[I⁻]₀ (M)	[OCl⁻]₀ (M)	Initial Rate $\left(\frac{mol}{L \cdot s}\right)$
1	0.12	0.18	7.91×10 ⁻²
2	0.060	0.18	3.95×10 ⁻²
3	0.030	0.090	9.88×10 ⁻²
4	0.24	0.090	7.91×10 ⁻²

From experiments 1 and 2 ([OCl⁻]_o is kept constant) as the initial concentration of I⁻ is doubled, the initial rate of the reaction doubles $\left(\frac{7.91 \times 10^{-2}}{3.95 \times 10^{-2}}=2.0\right)$; therefore, the reaction is first order with respect to I⁻.

$$Rate = k[I^-][OCl^-]^y$$

You must find the order of OCl⁻ the long way.

Divide the 2 equations (in which the [OCI⁻] changes) by each other.

$$\frac{7.91 \times 10^{-2} \frac{mol}{L \cdot s}}{9.88 \times 10^{-3} \frac{mol}{L \cdot s}} = \frac{k(0.12)(0.18 M)^{y}}{k(0.030)(0.090 M)^{y}}$$

$$2.0 = 2.0^{y}$$

$$y = 1$$

$$Rate = k[I^{-}][OCl^{-}]$$

$$Bate = k[I^{-}][OCl^{-}]$$

$$7.91 \times 10^{-2} \frac{mol}{L \cdot s} = k(0.12 M)(0.18 M)$$

$$k = 3.7 \frac{L}{mol \cdot s}$$

$$c) \qquad Rate = k[I^{-}][OCl^{-}] = (3.7 \frac{L}{mol \cdot s})(0.15 M)(0.15 M) = 0.082 \frac{mol}{L \cdot s}$$

20. General Rate Law

Rate	$Rate = k[N_2O_5]^x$								
	Experiment	[N ₂ O ₅] _o (M)	Initial Rate $\left(\frac{mol}{L:s}\right)$						
	1	0.0750	8.90×10 ⁻⁴						
	2	0.190	2.26×10 ⁻³						
	3	0.275	3.26×10⁻³						
	4	0.410	4.85×10 ⁻³						

You must solve this problem the long way.

$$8.90 \times 10^{-4} \frac{mol}{L \cdot s} = k(0.0750 M)^{x}$$
$$2.26 \times 10^{-3} \frac{mol}{L \cdot s} = k(0.190 M)^{x}$$

Divide the 2 equations by each other.

$$\frac{8.90 \times 10^{-4} \frac{mol}{L \cdot s}}{2.26 \times 10^{-3} \frac{mol}{L \cdot s}} = \frac{k(0.0750 M)^{x}}{k(0.190 M)^{x}}$$

$$0.394 = 0.395^{x}$$

$$x = 1$$

$$Rate = k[N_{2}O_{4}]$$

$$8.90 \times 10^{-4} \frac{mol}{L \cdot s} = k(0.0750 M)$$

$$k = 0.0119 \frac{1}{s}$$

21. a) **General Rate Law**

b)

k

 $Rate = k[NOCI]^{x}$

	Experiment	$[NOCI]_{o}\left(\frac{molecules}{cm^{3}}\right)$	Initial Rate $\left(\frac{molecules}{cm^{3}\cdot s}\right)$				
	1	3.0×10 ¹⁶	5.98×10 ⁴				
	2	2.0×10 ¹⁶	2.66×10 ⁴				
	3	1.0×10 ¹⁶	6.64×10 ³				
	4	4.0×10 ¹⁶	1.06×10 ⁵				

From experiments 2 and 3, as the initial concentration of NOCl is doubled, the initial rate of the reaction quadruples $\left(\frac{2.66 \times 10^4}{6.64 \times 10^3} = 4.0\right)$; therefore, the reaction is second order with respect to NOCI.

 $Rate = k[NOCl]^{2}$ 5.98 × 10⁴ $\frac{molecules}{cm^{3} \cdot s} = k(3.0 \times 10^{16} \frac{molecules}{cm^{3}})^{2}$

$$k = 6.6 \times 10^{-29} \frac{cm^3}{molecules \cdot s}$$

$$k = 6.6 \times 10^{-29} \frac{cm^3}{molecules \cdot s} \left(\frac{6.022 \times 10^{23} \text{ molecules}}{1 \text{ mol}}\right) \left(\frac{1 \text{ L}}{10^3 \text{ cm}^3}\right) = 4.0 \times 10^{-8} \frac{L}{mol \cdot s}$$

$Rate = k[Hb]^{x}[CO]^{y}$								
Experiment	$[Hb]_{o}\left(\frac{\mu mol}{L}\right)$	$[CO]_{o}\left(\frac{\mu mol}{L}\right)$	Initial Rate $\left(\frac{\mu mol}{L:s}\right)$					
1	2.21	1.00	0.619					
2	4.42	1.00	1.24					
3	4.42	3.00	3.71					

From experiments 1 and 2 ([CO]_o is kept constant) as the initial concentration of Hb is doubled, the initial rate of the reaction doubles $\left(\frac{1.24}{0.619}=2.00\right)$; therefore, the reaction is first order with respect to Hb.

You cannot use the shortcut to calculate the order with respect to [CO] Find 2 equations where the concentration of Hb is constant

$$1.24 \frac{\mu mol}{L \cdot s} = k \left(4.42 \frac{\mu mol}{L} \right) \left(1.00 \frac{\mu mol}{L} \right)^3$$
$$3.71 \frac{\mu mol}{L \cdot s} = k \left(4.42 \frac{\mu mol}{L} \right) \left(3.00 \frac{\mu mol}{L} \right)^3$$

Divide the 2 equations by each other.

$$\frac{1.24 \ \frac{\mu mol}{L \cdot s} = k \left(4.42 \ \frac{\mu mol}{L}\right) \left(1.00 \ \frac{\mu mol}{L}\right)^{y}}{3.71 \ \frac{\mu mol}{L \cdot s} = k \left(4.42 \ \frac{\mu mol}{L}\right) \left(3.00 \ \frac{\mu mol}{L}\right)^{y}}{0.33 = \frac{\left(1.00 \ \frac{\mu mol}{L}\right)^{y}}{\left(3.00 \ \frac{\mu mol}{L}\right)^{y}} = (0.33)^{y}}{\left(3.00 \ \frac{\mu mol}{L}\right)^{y}}$$
$$y = 1$$

The reaction is 1st order with respect to CO

b)
$$Rate = k[Hb][CO]$$

c) $Rate = k[Hb][CO]$
 $0.619 \frac{\mu mol}{L \cdot s} = k \left(2.21 \frac{\mu mol}{L}\right) \left(1.00 \frac{\mu mol}{L}\right)$
 $k = 0.280 \frac{L}{\mu mol \cdot s}$
d) $Rate = 0.280 \frac{L}{\mu mol} [Hb][CO] = \left(0.280 \frac{L}{L}\right) \left(3.36 \frac{\mu mol}{L}\right) (2.21 \frac{\mu mol}{L})$

d)
$$Rate = 0.280 \frac{L}{\mu mol \cdot s} [Hb][CO] = \left(0.280 \frac{L}{\mu mol \cdot s}\right) \left(3.36 \frac{\mu mol}{L}\right) \left(2.40 \frac{\mu mol}{L}\right) = 2.26 \frac{\mu mol}{L \cdot s}$$

23. General a)

 $Rate = k[ClO_2]^x[OH^-]^y$ Initial Rate $\left(\frac{mol}{Ls}\right)$ $[OH^{-}]_{\circ}(M)$ Experiment [ClO₂]_o (M) 0.0500 0.100 5.75×10⁻² 1 2 2.30×10⁻¹ 0.100 0.100 3 1.15×10⁻¹ 0.100 0.0500

From experiments 1 and 2 ([OH⁻]_o is kept constant) as the initial concentration of ClO₂ is doubled, the initial rate of the reaction quadruples $\left(\frac{2.30 \times 10^{-1}}{5.75 \times 10^{-2}} = 4.00\right)$; therefore, the reaction is second order with respect to ClO₂.

From experiments 2 and 3 ([ClO₂]_o is kept constant) as the initial concentration of OH⁻ is doubled, the initial rate of the reaction doubles $\left(\frac{2.30 \times 10^{-1}}{1.15 \times 10^{-1}}=2.00\right)$; therefore, the reaction is first order with respect to OH⁻.

 $Rate = k[ClO_2]^2[OH^-]$

Find k

Find k

$$5.75 \times 10^{-2} \frac{mol}{L \cdot s} = k(0.0500 \, M)^2 (0.100 \, M)$$

$$k = 230. \frac{L^2}{mol^2 \cdot s}$$

$$Rate = 230. \frac{L^2}{mol^2 \cdot s} [ClO_2]^2 [OH^-]$$
b)
$$Rate = 230. \frac{L^2}{mol^2 \cdot s} (0.175 \, M)^2 (0.0844 \, M) = 0.594 \frac{mol}{L \cdot s}$$

30.

b)

a) Because the plot of
$$\frac{1}{[A]}$$
 verse time was linear the rate law is a second order rate law.

$$Rate = k[A]^{2}$$

$$-\frac{d[A]}{dt} = k[A]^{2}$$

$$\frac{1}{[A]^{2}}d[A] = -kdt$$

$$\int_{[A]^{\circ}}^{[A]} \frac{1}{[A]^{2}}d[A] = \int_{0}^{t} -kdt$$

$$-\frac{1}{[A]} + \frac{1}{[A]^{\circ}} = -kt + 0$$

$$\frac{1}{[A]} = kt + \frac{1}{[A]^{\circ}} \text{ (integrated rate law)}$$

The rate constant is the slope of the line $k = 3.60 \times 10^{-2} \frac{L}{mol \cdot s}$
 $Rate = 3.60 \times 10^{-2} \frac{L}{mol \cdot s}[A]^{2} \text{ (rate law)}$

b) The half-life is the amount of time it takes for ½ of the original concentration to react.

$$\frac{1}{1} = kt + \frac{1}{1}$$

$$\begin{bmatrix} A \end{bmatrix} & 1 & [A]_{\circ} \\ \frac{1}{0.5(2.80 \times 10^{-3} M)} = \left(3.60 \times 10^{-2} \frac{L}{mol \cdot s}\right)t + \frac{1}{2.80 \times 10^{-3} M} \\ t = 9920 s \\ \frac{1}{[A]} = kt + \frac{1}{[A]_{\circ}} \\ \frac{1}{7.00 \times 10^{-4} M} = \left(3.60 \times 10^{-2} \frac{L}{mol \cdot s}\right)t + \frac{1}{2.80 \times 10^{-3} M} \\ t = 29,800 s$$

31. a) Because the plot of ln[A] verses t is linear, this is a 1st order rate law.
Rate = k[A]

$$-\frac{d[A]}{dt} = k[A]$$

$$\frac{1}{[A]}d[A] = -kdt$$

$$\int_{[A]_{\circ}}^{[A]} \frac{1}{[A]}d[A] = -\int_{0}^{t} kdt$$

$$ln[A] - ln[A]_{\circ} = -kt + 0$$

$$ln[A] = -kt + ln[A]_{\circ} \text{ (integrated rate law)}$$

The rate constant is the negative slope of the line
$$k = 2.97 \times 10^{-2} \frac{1}{min}$$

 $Rate = 2.97 \times 10^{-2} \frac{1}{min} [A]$ (rate law)
 $ln[A] = -kt + ln[A]_{\circ}$

$$ln\left(\frac{1}{2}(2.00 \times 10^{-2} M)\right) = -\left(2.97 \times 10^{-2} \frac{1}{min}\right)t + ln(2.00 \times 10^{-2} M)$$

$$t = 23.3 min$$

$$ln[A] = -kt + ln[A]_{\circ}$$

$$ln(2.50 \times 10^{-3} M) = -\left(2.97 \times 10^{-2} \frac{1}{min}\right)t + ln(2.00 \times 10^{-2} M)$$

$$t = 70.0 min$$

32.

a)

b)

Because the plot of
$$[C_2H_5OH]$$
 verses t is linear, this is a 0th order rate law
 $Rate = k$
 $-\frac{d[C_2H_5OH]}{dt} = k$
 $d[C_2H_5OH] = -kdt$
 $\int_{[C_2H_5OH]^{\circ}}^{C_2H_5OH} d[C_2H_5OH] = -\int_{0}^{t} kdt$
 $[C_2H_5OH] - [C_2H_5OH]^{\circ} = -kt + 0$
 $[C_2H_5OH] = -kt + [C_2H_5OH]^{\circ}$ (integrated rate law)
The rate constant equals the negative slope of the line; $k = 4.00 \times 10^{-5} \frac{mol}{Ls}$
 $Rate = 4.00 \times 10^{-5} \frac{mol}{Ls}$ (rate law)
 $[C_2H_5OH] = -kt + [C_2H_5OH]^{\circ}$
 $\frac{1}{2}(1.25 \times 10^{-2} M) = -(4.00 \times 10^{-5} \frac{mol}{Ls})t + (1.25 \times 10^{-2} M)$

t = 156 sc) Since this is a 0th order rate law (which means that the rate is independent of concentration), the amount of time that it takes to decompose the total amount of C₂H₅OH is just double the half-life.

$$t = 2(156 s) = 312 s$$

Or

$$0 = -(4.00 \times 10^{-5} \frac{mol}{Ls})t + (1.25 \times 10^{-2} M)$$

$$t = 312 s$$





Time (c)		Difference		Difference	[LI O]-1	Difference
Time (S)		between points		between points		between points
0	1.00	0.59-1.00=-0.41	0.00	-0.53-0.00=-0.53	1.00	1.7-1.00=0.7
600	0.59	-0.22	-0.53	-0.46	1.7	1.0
1200	0.37	-0.15	-0.99	-0.5	2.7	1.8
1800	0.22	-0.09	-1.5	-0.5	4.5	3.3
2400	0.13	-0.05	-2.0	-0.5	7.7	4.3
3000	0.082		-2.5		12	

If you do not have a graphing calculator look at the spacing between the evenly spaces times to determine the order.

Since the all the differences between $ln[H_2O_2]$ are all approximately -0.5 this will be a straight line and the reaction is 1^{st} order.

Differential Rate Law

 $Rate = k[H_2O_2]$ Integrated Rate Law

 $ln[H_2O_2] = -kt + ln[H_2O_2]_{\circ}$

The slope of the line will equal –k.

$$slope = \frac{rise}{run} = \frac{ln(0.050 M) - ln(1.00 M)}{3,600 s - 0 s} = -8.3 \times 10^{-4} \frac{1}{s} = -k$$

$$k = 8.3 \times 10^{-4} \frac{1}{s}$$

Calculate the concentration of H_2O_2 after 4000. s.

$$ln[H_2O_2] = -\left(8.3 \times 10^{-4} \frac{1}{s}\right)(4,000 \, s) + ln(1.00 \, M)$$
$$[H_2O_2] = 0.036 \, M$$

[A] vs. t, In[A] vs. t, and [A]⁻¹ vs. t



Since the plot of [A]⁻¹ vs. t is linear, this is a 2nd order rate law If you do not have a graphing calculator look at the spacing between the evenly spaces times to determine the order. You must have at least 3 points.

		Difference		Difference	[NO 1-1	Difference
Time (S)		between points		between points		between points
0	0.500	0.25-0.50=-0.25	-0.693	-1.39-0.693=-0.69	2.00	4.00-2.00=2.00
9.00×10 ³	0.250	-0.076	-1.39	-0.36	4.00	1.75
1.80×10 ⁴	0.174		-1.75		5.75	

This problem it is a little hard to determine. (I will not give you something this hard on an exam.) The difference between the difference between the [NO₂] points is 0.17 over a concentration range of 0.326 making the difference between differences $52\% \left(\frac{0.17}{0.326}100\% = 52\%\right)$ of the

range. The difference between the difference between the $ln[NO_2]$ is 0.33 over a $ln[NO_2]$ range of -1.06 making the difference between differences 31% $\left(\frac{0.33}{1.06}100\% = 33\%\right)$ of the range. The difference between the difference between $[NO_2]^{-1}$ is 0.25 over a range of 3.75 making the difference between differences 6% $\left(\frac{0.25}{3.75}100\% = 6\%\right)$ of the range. The graph $[NO_2]^{-1}$ has the smallest difference between differences, when you take the size of the range into account, the order is 2nd order.

Differential Rate Law

Plot

 $Rate = k[NO_2]^2$ Integrated Rate Law

$$\frac{1}{[NO_2]} = kt + \frac{1}{[NO_2]}$$

The slope of the line is the rate constant

$$slope = \frac{rise}{run} = \frac{\frac{1}{0.174 M} - \frac{1}{0.500 M}}{1.80 \times 10^4 s - 0 s} = 2.08 \times 10^{-4} \frac{L}{mol \cdot s} = k$$
$$\frac{1}{[NO_2]} = \left(2.08 \times 10^{-4} \frac{L}{mol \cdot s}\right)t + \frac{1}{[NO_2]_{\circ}}$$
$$\frac{1}{[NO_2]} = \left(2.08 \times 10^{-4} \frac{L}{mol \cdot s}\right)(2.70 \times 10^4 s) + \frac{1}{0.500 M} = 7.62 \frac{L}{mol}$$
$$[NO_2] = 0.131 M$$

36. a)

[O] vs. t, ln[O] vs. t, and [O]⁻¹vs. t



Since ln[O] vs. t is linear, the rate expression is 1st order with respect to O. If you do not have a graphing calculator look at the spacing between the evenly spaces times to determine the order.

Time (c)	[0]	Difference		Difference	[0]-1	Difference
rime (s)	[U]	between points	IN[U]	between points	[0] -	between points
0	5.0×10 ⁹	1.9×10 ⁹ -5.0×10 ⁹	22	21-22=-1.0	2.0×10 ⁻¹⁰	5.2×10 ⁻¹⁰ -2.0×10 ⁻¹⁰
		=-3.1×10 ⁹				= 3.2×10 ⁻¹⁰
0.010	1.9×10 ⁹	-1.2×10 ⁹	21	-1.0	5.2×10 ⁻¹⁰	9.8×10 ⁻¹⁰
0.020	6.8×10 ⁸	-4.3×10 ⁸	20.	-1.0	1.5×10 ⁻⁹	2.5×10 ⁻⁹
0.030	2.5×10 ⁸		19		4.0×10 ⁻⁹	

Since the all the differences between $ln[H_2O_2]$ are all approximately -1.0 this will be a straight line and the reaction is 1^{st} order.

Differential Rate Law

b) Overall Rate Law

$$Rate = k[O][NO_2]$$

Because the concentration of [NO_2] >>[O] this can be turned into a pseudo rate law
$$Rate = k'[O]$$

 $k' = k[NO_2]$

Determine k' using the 1st order integrated rate law

 $ln[0] = -k't + ln[0]_{\circ}$

Therefore, the slope of the line is -k'

$$slope = \frac{rise}{run} = \frac{ln(2.5 \times 10^8 \frac{atoms}{cm^3}) - ln(5.0 \times 10^9 \frac{atoms}{cm^3})}{3.0 \times 10^{-2} s - 0 s} = -1.0 \times 10^2 \frac{1}{s} = -k'$$

k' = 1.0 × 10² $\frac{1}{s}$

Find k

$$k' = k[NO_2]$$

$$\left(1.0 \times 10^2 \frac{1}{s}\right) = k[NO_2]$$

$$k = 1.0 \times 10^{-11} \frac{cm^3}{molecules \cdot s}$$

38. a) The order of the reaction with respect to A is 2nd order because the plot of [A]⁻¹ vs. t is linear.

The integrated rate law is.

$$\frac{1}{[A]} = kt + \frac{1}{[A]}$$

Therefore, the $[A]_0^{-1}$ is the y intercept. $[A]_0^{-1} = 10 \frac{L}{mol}$ and $[A]_0 = 0.1 \text{ M}$

b)
$$\frac{1}{[A]} = kt + \frac{1}{[A]_{\circ}}$$

$$k = slope = \frac{rise}{run} = \frac{70 \frac{L}{mol} - 20 \frac{L}{mol}}{6 s - 0 s} = 10 \frac{L}{mol \cdot s}$$

$$\frac{1}{[A]} = \left(10 \frac{L}{mol \cdot s}\right) (9 s) + 10 \frac{L}{mol} = 100 \frac{L}{mol}$$

$$[A] = 0.01 M$$
c) Calculate the time for the 1st half-life ([A] 0.1 \rightarrow 0.05)
$$\frac{1}{0.05 M} = \left(10 \frac{L}{mol \cdot s}\right) t + \frac{1}{0.1 M}$$

$$t = 1 s$$
Calculate the time for the 2nd half-life
$$\frac{1}{0.025 M} = \left(10 \frac{L}{mol \cdot s}\right) t + \frac{1}{0.05 M}$$

$$t = 2 s$$
Calculate the time for the 3rd half-life

$$\frac{1}{0.0125 M} = \left(10 \frac{L}{mol \cdot s}\right) t + \frac{1}{0.025 M} t = 4 s$$

39. a) Plot [NO] vs. t, $\ln[NO]$ vs. t, and, $[NO]^{-1}$ vs. t 8.E+08 6.E+08 4.E+08 4.E+08 6.E+08 6.E+08 6.E+08 6.E+08 6.E+08 6.E+08 19.5 19.5 19.5

2.E+08

0.E+00

time



Since the plot of ln[NO] vs. t is linear, the rate law is 1st order with respect to NO.

Time (s)		Difference		Difference	[NO]-1	Difference	
Time (3)		between points		between points		between points	
0	6.0×10 ⁸	2.4×10 ⁸ -6.0×10 ⁸	20	19-20=-1.0	1.7×10 ⁻⁹	4.2×10 ⁻⁹ -1.7×10 ⁻⁹	
		=-3.6×10 ⁸				= 2.5×10 ⁻⁹	
500	2.4×10 ⁸	-1.4×10 ⁸	19	-1.0	4.2×10 ⁻⁹	5.8×10 ⁻⁹	
1000	9.9×10 ⁷		18		1.0×10 ⁻⁸		

If you do not have a graphing calculator look at the spacing between the evenly spaces times to determine the order.

Since the all the differences between ln[NO] are all approximately -1.0 this will be a straight line and the reaction is 1st order.

Plot

 $[O_3]$ vs. t, $ln[O_3]$ vs. t, and $[O_3]^{-1}$ vs. t



Since plot of $In[O_3]$ vs. t is linear, the rate law is 1^{st} order with respect to O_3

If you do not have a graphing calculator look at the spacing between the evenly spaces times to determine the order.

Time (c)	[0]]	Difference		Difference	[O]-1	Difference
Time (s)	[U ₃]	between points	III[U ₃]	between points	[U ₃]	between points
0	1.0×10 ¹⁰	7.0×10 ⁹ -1.0×10 ¹⁰	23.0	22.7-23.0=-0.3	1.0×10 ⁻¹⁰	1.4×10 ⁻¹⁰ -1.0×10 ⁻¹⁰
		=-3.0×10 ⁹				= 4.0×10 ⁻¹¹
100	7.0×10 ⁹	-2.1×10 ⁹	22.7	-0.4	1.4×10 ⁻¹⁰	6.0×10 ⁻¹¹
200	4.9×10 ⁹	-1.5×10 ⁹	22.3	-0.4	2.0×10 ⁻¹⁰	9.0×10 ⁻¹¹
300	3.4×10 ⁹		21.9		2.9×10 ⁻¹⁰	

Since the all the differences between $ln[O_3]$ are all approximately -0.4 this will be a straight line and the reaction is 1^{st} order.

b) Rate Law

 $Rate = k[NO][O_3]$

c) When the [NO] data was taken the concentration of $[O_3] >> [NO]$. Therefore, a pseudo rate law can be written.

$$Rate = k'[NO]$$
$$k' = k[O_3]$$

Since the reaction was first order with respect to [NO] the slope of the line equals -k'

 $k' = -slope = -\frac{rise}{run} = -\frac{ln(9.9 \times 10^7 \frac{molecules}{cm^3}) - ln(6.0 \times 10^8 \frac{molecules}{cm^3})}{1000.ms - 0 ms} = 0.0018 \frac{1}{ms}$ When the [O₃] data was taken the concentration of [NO]>>[O₃]. Therefore, a pseudo

rate law can be written.

$$Rate = k''[O_3]$$
$$k'' = k[NO]$$

Since the reaction was first order with respect to $[\mathsf{O}_3]$ the slope of the line equals $-k^{\prime\prime}$

$$k'' = -slope = -\frac{rise}{run} = -\frac{ln(3.4 \times 10^9 \frac{molecules}{cm^3}) - ln(1.0 \times 10^{10} \frac{molecules}{cm^3})}{300.ms - 0 ms}$$
$$= 0.0036 \frac{1}{ms}$$

d) You can solve this using either of the two data sets. In both data sets the reactions are pseudo 1st order system. Overall rate = pseudo 1st order rate Using data set 1 [O₃] held constant

$$k[NO][O_3] = k'[NO]$$

$$k = \frac{k'}{[O_3]} = \frac{0.0018 \frac{1}{ms}}{1.0 \times 10^{14} \frac{molecules}{cm^3}} = 1.8 \times 10^{-17} \frac{cm^3}{molecules \cdot ms}$$

Using data set 2 [NO] held constant

$$k[NO][O_3] = k''[O_3]$$

$$k = \frac{k''}{[NO]} = \frac{0.0036 \frac{1}{ms}}{2.0 \times 10^{14} \frac{molecules}{cm^3}} = 1.8 \times 10^{-17} \frac{cm^3}{molecules \cdot ms}$$

43.
$$ln[PH_{3}] = -kt + ln[PH_{3}]_{o}$$
$$ln(0.250 M) = -k(120.s) + ln(1.00 M)$$
$$k = 0.0116 \frac{1}{s}$$
$$ln[PH_{3}] = -\left(0.0116 \frac{1}{s}\right)t + ln[PH_{3}]_{o}$$
$$ln(0.350 M) = -\left(0.0116 \frac{1}{s}\right)t + ln(2.00 M)$$
$$t = 151 s$$

47. a) Calculate k

$$ln[A] = -kt + ln[A]_{o}$$

$$ln(0.250[A]_{o}) = -k(320.s) + ln[A]_{o}$$

$$ln\left(\frac{0.250[A]_{o}}{[A]_{o}}\right) = -k(320.s)$$

$$k = 0.00433\frac{1}{s}$$
Calculate time for 1st half life

$$ln\left(\frac{1}{2}[A]_{o}\right) = -\left(0.00433\frac{1}{s}\right)t + ln[A]_{o}$$

$$ln\left(\frac{1}{2}[A]_{o}\right) = -\left(0.00433\frac{1}{s}\right)t$$

$$t = 159 s$$
Calculate time for the 2nd half life

$$ln\left(\frac{1}{4}[A]_{o}\right) = -\left(0.00433\frac{1}{s}\right)t + ln\left(\frac{1}{2}[A]_{o}\right)$$

$$ln\left(\frac{1}{4}[A]_{o}\right) = -\left(0.00433\frac{1}{s}\right)t + ln\left(\frac{1}{2}[A]_{o}\right)$$

$$ln\left(\frac{1}{4}[A]_{o}\right) = -\left(0.00433\frac{1}{s}\right)t + ln\left(\frac{1}{2}[A]_{o}\right)$$

$$ln\left(\frac{100[A]_{o}}{1}\right) = -\left(0.00433\frac{1}{s}\right)t + ln[A]_{o}$$

$$ln\left(\frac{0.100[A]_{o}}{[A]_{o}}\right) = -\left(0.00433\frac{1}{s}\right)t + ln[A]_{o}$$

$$ln\left(\frac{0.100[A]_{o}}{[A]_{o}}\right) = -\left(0.00433\frac{1}{s}\right)t + ln[A]_{o}$$

$$ln\left(\frac{0.100[A]_{o}}{[A]_{o}}\right) = -\left(0.00433\frac{1}{s}\right)t + ln[A]_{o}$$

48. Since the time of the half-life doubles every successive half-life, the reaction is a 2nd order reaction

a)
$$\frac{1}{[A]} = kt + \frac{1}{[A]_o}$$
$$\frac{1}{0.05 M} = k(10.0 \min) + \frac{1}{0.10 M}$$
$$k = 1.0 \frac{L}{mol \cdot min}$$
$$\frac{1}{[A]} = \left(1.0 \frac{L}{mol \cdot min}\right)(80.0 \min) + \frac{1}{0.10 M} = 90.\frac{L}{mol}$$
$$[A] = 0.011 M$$
b)
$$\frac{1}{[A]} = \left(1.0 \frac{L}{mol \cdot min}\right)(30.0 \min) + \frac{1}{0.10 M} = 40.\frac{L}{mol}$$
$$[A] = 0.025 M$$

52. The problem wants you to find the time when [A] = 4.00[B]. Known

$$\begin{aligned} k_{A} &= 4.50 \times 10^{-4} \frac{1}{s} \\ k_{B} &= 3.70 \times 10^{-3} \frac{1}{s} \\ \text{Both } 1^{\text{st}} \text{ order reactions} \end{aligned}$$

$$\begin{aligned} & [A]_{o} &= [B]_{o} \\ ln[A] &= -kt + ln[A]_{o} \\ ln[B] &= -kt + ln[B]_{o} \\ ln[B] &= -kt + ln[B]_{o} \end{aligned}$$

$$\begin{aligned} & Plug \text{ in}[B]_{o} \text{ for}[A]_{o} \text{ and}[A] &= 4.00[B] \text{ for}[A] \text{ and solve for } [B] \\ ln(4.00[B]) &= -k_{A}t + ln[B]_{o} \\ 4.00[B] &= e^{-k_{A}t + ln[B]_{o}} \\ & [B] &= \frac{e^{-k_{A}t + ln[B]_{o}}}{4.00} \end{aligned}$$

$$\begin{aligned} & Plug \text{ into equation for } [B] \text{ and solve for t} \\ & ln[B] &= -k_{B}t + ln[B]_{o} \\ & ln\left(\frac{e^{-k_{A}t + ln[B]_{o}}}{4.00}\right) &= -k_{B}t + ln[B]_{o} \\ & ln\left(\frac{e^{-k_{A}t + ln[B]_{o}}}{4.00}\right) &= -k_{B}t + ln[B]_{o} \\ & ln(e^{-k_{A}t + ln[B]_{o}}) - ln(4.00) &= -k_{B}t + ln[B]_{o} \\ & -k_{A}t + ln[B]_{o} - ln(4.00) &= -k_{B}t \\ & -ln(4.00) &= (-k_{B} + k_{A})t \\ & t &= \frac{-ln(4.00)}{-k_{B} + k_{A}} &= \frac{-ln(4.00)}{-3.70 \times 10^{-3} \frac{1}{s} + 4.50 \times 10^{-4} \frac{1}{s}} = 427 \ s \end{aligned}$$

54. The concentrations of B and C are so much larger than A, therefore, during the course of the reaction they do not effectively change making this a pseudo 1^{st} order reaction. The rate of the pseudo 1^{st} order reaction is equal to the rate of the overall reaction times $[B]^2$.

a)
$$rate = k[A][B]^{2} = k'[A]$$
$$k' = k[B]^{2}$$
$$ln[A] = -k't + ln[A]_{o}$$
$$ln(3.8 \times 10^{-3} M) = -k'(8.0 s) + ln(1.0 \times 10^{-2} M)$$
$$k' = 0.12\frac{1}{s}$$

$$k' = k[B]^{2}$$

$$k = \frac{k'}{[B]^{2}} = \frac{0.12 \frac{1}{s}}{(3.0 M)^{2}} = 0.013 \frac{L^{2}}{mol^{2} \cdot s}$$
b)
$$ln[A] = -(0.12 \frac{1}{s})t + ln[A]_{o}$$

$$ln(0.0050 M) = -(0.12 \frac{1}{s})t + ln(1.0 \times 10^{-2} M)$$

$$t = 5.8 s$$
c)
$$ln[A] = -(0.12 \frac{1}{s})t + ln[A]_{o}$$

$$ln[A] = -(0.12 \frac{1}{s})(13.0 s) + ln(1.0 \times 10^{-2} M)$$

$$[A] = 0.0021 M$$
d)
The concentration of C is the $[C]_{o} - 2\Delta[A]$

$$\Delta[A] = 1.0 \times 10^{-2} M - 0.0021 M = 0.008 M$$

$$[C] = [C]_{o} - 2\Delta[A] = 2.0 M - 2(0.008 M) = 2.0 M$$
This should not be a surprising answer because in order to hardow the surprise of the surprise of

This should not be a surprising answer because in order to have a pseudo 1st order reaction with respect to A, the concentration of C must be essentially constant.

- 56. a) Elementary Step: An individual reaction in a proposed reaction mechanism. The rate law can be written from the coefficients in the balanced equation
 - b) Molecularity: The number of reactant molecules (or free atoms) taking part in an elementary reaction. This is also the number of species that must collide in order to produce the reaction represented by an elementary reaction.
 - c) Reaction Mechanism: The pathway that is proposed for an overall reaction and accounts for the experimental rate law.
 - d) Intermediate: A species that is produced and consumed during a reaction but does not appear in the overall chemical equation.
 - e) Rate Determining Step: The elementary reaction that governs the rate of the overall reaction. This is the slowest elementary reaction that occurs in a mechanism.
- 59. For elementary reactions the rate is just equal to the rate constant times the concentration of the reactants.
 - a) $Rate = k[CH_3NC]$
 - b) $Rate = k[O_3][NO]$
 - c) $Rate = k[O_3]$
 - d) $Rate = k[O_3][O]$
 - e) $Rate = k \begin{bmatrix} 14 \\ 6 \end{bmatrix}$
- 60. The rate law found in problem 33 was

$$Rate = k[H_2O_2]$$

In order for this to be the rate, the first step would have to be the rate determining step. Overall Reaction

 $2H_2O_2 \rightarrow 2H_2O + O_2$

61. $Rate = k[C_4H_9Br]$ Overall Reaction $C_4H_9Br + 2H_2O \rightarrow Br^- + C_4H_9OH + H_3O^+$ Intermediates $C_4H_9^+ \text{ and } C_4H_9OH_2^+$

- 63. The rate of a reaction is dependent on the slowest step.
 - a) $Rate = k[NO][O_2]$ The mechanism is not consistent with rate law.
 - b) $Rate = k_2[NO_3][NO]$

 NO_3 is an intermediate, therefore, it needs to be eliminated from the rate equation. Use equilibrium to eliminate

$$\begin{aligned} &k_1[NO][O_2] = k_{-1}[NO_3]\\ &[NO_3] = \frac{k_1[NO][O_2]}{k_{-1}}\\ &Rate = k_2[NO_3][NO] = k_2[NO]\frac{k_1[NO][O_2]}{k_{-1}} = \frac{k_2k_1[NO]^2[O_2]}{k_{-1}} = k[NO]^2[O_2] \end{aligned}$$

The mechanism is consistent with rate law.

- c) $Rate = k[NO]^2$ The mechanism is not consistent with rate law.
- d) In order for a mechanism to be plausible the elementary reactions must add up to the overall reaction. These elementary reactions do not add up to the overall reaction. In fact the middle reaction is not even balanced.

65. $Rate = k_3[Br^-][H_2BrO_3^+]$

 $H_2BrO_3^+$ is an intermediate therefore, needs to be eliminated from the rate law. Use equilibrium to eliminate the intermediate.

$$k_{2}[HBrO_{3}][H^{+}] = k_{-2}[H_{2}BrO_{3}^{+}]$$
$$[H_{2}BrO_{3}^{+}] = \frac{k_{2}[HBrO_{3}][H^{+}]}{k_{-2}}$$
$$Rate = k_{3}[Br^{-}][H_{2}BrO_{3}^{+}] = \frac{k_{2}k_{3}[Br^{-}][HBrO_{3}][H^{+}]}{k_{-2}}$$

 $HBrO_3$ is an intermediate therefore, needs to be eliminated from the rate law. Use equilibrium to eliminate the intermediate.

$$\begin{aligned} k_1[BrO_3^-][H^+] &= k_{-1}[HBrO_3]\\ [HBrO_3] &= \frac{k_1[BrO_3^-][H^+]}{k_{-1}}\\ Rate &= \frac{k_2k_3[Br^-][HBrO_3][H^+]}{k_{-2}} = \frac{k_1k_2k_3[Br^-][BrO_3^-][H^+]^2}{k_{-1}k_{-2}} = k[Br^-][BrO_3^-][H^+]^2 \end{aligned}$$

68.

a)

$$Rate = k_3[COCl][Cl_2]$$

COCI is an intermediate, therefore, it needs to be eliminated from the rate law. Use equilibrium to eliminate the intermediate.

$$k_{2}[CO][Cl] = k_{-2}[COCl]$$
$$[COCl] = \frac{k_{2}[CO][Cl]}{k_{-2}}$$
$$Rate = k_{3}[COCl][Cl_{2}] = \frac{k_{3}k_{2}[CO][Cl][Cl_{2}]}{k_{-2}}$$

Cl is an intermediate, therefore, it needs to be eliminated from the rate law. Use equilibrium to eliminate the intermediate.

$$k_{1}[Cl_{2}] = k_{-1}[Cl]^{2}$$

$$[Cl] = \frac{k_{1}^{1/2}[Cl_{2}]^{1/2}}{k_{-1}^{1/2}}$$

$$Rate = \frac{k_{3}k_{2}[CO][Cl][Cl_{2}]}{k_{-2}} = \frac{k_{3}k_{2}[CO][Cl_{2}]k_{1}^{1/2}[Cl_{2}]^{1/2}}{k_{-2}k_{-1}^{1/2}} = \frac{k_{3}k_{2}k_{1}^{1/2}[CO][Cl_{2}]^{3/2}}{k_{-2}k_{-1}^{1/2}}$$

$$Rate = k[CO][Cl_{2}]^{3/2}$$

b) COCI and CI are intermediates

69.

a)

$$MoCl_5$$
 is an intermediate

b)
$$\frac{d[NO_2]}{dt} = k_2[NO_3^-][MoCl_5^-]$$

Use the steady state approximation to eliminate the intermediate, rate of formation = rate of consumption

$$\begin{split} k_1[MoCl_6^{2-}] &= k_{-1}[MoCl_5^{-}][Cl^{-}] + k_2[NO_3^{-}][MoCl_5^{-}] \\ [MoCl_5^{-}] &= \frac{k_1[MoCl_6^{2-}]}{k_{-1}[Cl^{-}] + k_2[NO_3^{-}]} \\ \frac{d[NO_2^{-}]}{dt} &= k_2[NO_3^{-}][MoCl_5^{-}] = \frac{k_1k_2[NO_3^{-}][MoCl_6^{2-}]}{k_{-1}[Cl^{-}] + k_2[NO_3^{-}]} \end{split}$$

70. Need to calculate the rate of decomposition of O_3

$$\frac{d[O_3]}{dt} = k_1[M][O_3] + k_2[O][O_3] - k_{-1}[O_2][O][M]$$

Note: Rate of decomposition=ways O_3 used up – ways O_3 forms O is an intermediate therefore need to remove it from the rate law.

Use the same steady state approximation to solve for [O]

$$k_{1}[M][O_{3}] = k_{-1}[O_{2}][O][M] + k_{2}[O][O_{3}]$$

$$[O] = \frac{k_{1}[M][O_{3}]}{k_{-1}[O_{2}][M] + k_{2}[O_{3}]}$$

$$-\frac{d[O_{3}]}{dt} = k_{1}[M][O_{3}] + k_{2}[O][O_{3}] - k_{-1}[O_{2}][O][M]$$

$$-\frac{d[O_{3}]}{dt} = k_{1}[M][O_{3}] + \frac{k_{1}k_{2}[M][O_{3}]^{2}}{k_{-1}[O_{2}][M] + k_{2}[O_{3}]} - \frac{k_{1}k_{-1}[O_{2}][M]^{2}[O_{3}]}{k_{-1}[O_{2}][M] + k_{2}[O_{3}]}$$

$$-\frac{d[O_{3}]}{dt} = \frac{k_{1}k_{-1}[O_{2}][M]^{2}[O_{3}] + k_{1}k_{2}[M][O_{3}]^{2} - k_{1}k_{-1}[O_{2}][M]^{2}[O_{3}]}{k_{-1}[O_{2}][M] + k_{2}[O_{3}]}$$

$$-\frac{d[O_{3}]}{dt} = \frac{k_{1}k_{-1}[O_{2}][M]^{2}[O_{3}] + k_{1}k_{2}[M][O_{3}]^{2} + k_{1}k_{2}[M][O_{3}]^{2} - k_{1}k_{-1}[O_{2}][M]^{2}[O_{3}]}{k_{-1}[O_{2}][M] + k_{2}[O_{3}]}$$

72. a) As the activation energy decreases the rate of the reaction goes up.

- b) As the temperature increases the molecules/atoms move faster and more collisions occur, therefore, the faster the rate of the reaction.
- c) As the frequency of collisions increases the rate of the reaction goes up.

d) As the orientation of collisions is more specific the rate of the reaction goes down.

79.
$$ln\left(\frac{k_{1}}{k_{2}}\right) = \frac{E_{a}}{R}\left(\frac{1}{T_{2}} - \frac{1}{T_{1}}\right)$$
$$ln\left(\frac{k_{1}}{3.52 \times 10^{-7} \frac{L}{mol \cdot s}}\right) = \frac{186 \frac{kJ}{mol}}{0.0083145 \frac{kJ}{mol \cdot K}} \left(\frac{1}{555 K} - \frac{1}{645 K}\right)$$
$$k_{1} = 9.75 \times 10^{-5} \frac{L}{mol \cdot s}$$

$$ln\left(\frac{k_{1}}{k_{2}}\right) = \frac{E_{a}}{R}\left(\frac{1}{T_{2}} - \frac{1}{T_{1}}\right)$$

$$ln\left(\frac{7.2 \times 10^{-4} \frac{1}{s}}{1.7 \times 10^{-2} \frac{1}{s}}\right) = \frac{E_{a}}{8.3145 \frac{J}{mol \cdot K}} \left(\frac{1}{720.K} - \frac{1}{660.K}\right)$$

$$E_{a} = 210,000 \frac{J}{mol}$$

$$ln\left(\frac{k_{1}}{k_{2}}\right) = \frac{E_{a}}{R} \left(\frac{1}{T_{2}} - \frac{1}{T_{1}}\right)$$

$$ln\left(\frac{k_{1}}{1.7 \times 10^{-2} \frac{L}{mol \cdot s}}\right) = \frac{210,000 \frac{J}{mol}}{8.3145 \frac{J}{mol \cdot K}} \left(\frac{1}{720.K} - \frac{1}{598 K}\right)$$

$$k_{1} = 1.3 \times 10^{-5} \frac{1}{s}$$

After each half-life the number of moles of iodoethane is halved. Therefore after 3 half-lives there is $\frac{1}{8}$ the number of moles of iodoethane that there was initially. For a gas, PV=nRT, therefore, since the volume, gas constant, and temperature are constant

$$\frac{\frac{P_1}{n_1} = \frac{P_2}{n_2}}{\frac{894 \ torr}{x} = \frac{P_2}{\frac{1}{8}x}}$$
$$\frac{P_2}{P_2} = 112 \ torr$$

$$ln\left(\frac{k_{1}}{k_{2}}\right) = \frac{E_{a}}{R}\left(\frac{1}{T_{2}} - \frac{1}{T_{1}}\right)$$

$$ln\left(\frac{7x}{x}\right) = \frac{5.40 \times 10^{4} \frac{J}{mol}}{8.3145 \frac{J}{mol \cdot K}} \left(\frac{1}{295 K} - \frac{1}{T_{1}}\right)$$

$$T_{1} = 324 K = 51^{\circ}\text{C}$$

a) $ln(k) = -\frac{E_a}{R} \left(\frac{1}{T}\right) + ln(A)$ Therefore, when the ln(k) is plotted vs. $\frac{1}{T}$ the slope of the line equals $-\frac{E_a}{R}$ $-\frac{E_a}{R} = -\frac{E_a}{8.3145 \frac{J}{mol \cdot K}} = -1.10 \times 10^4 K$ $E_a = 9.15 \times 10^4 \frac{J}{mol} = 91.5 \frac{kJ}{mol}$ b) When the ln(k) is plotted vs. $\frac{1}{T}$ the y intercept of the line equals ln(A) ln(A) = 33.5 $A = 3.54 \times 10^{14} \frac{1}{s}$ c) $ln(k) = -\frac{E_a}{R} \left(\frac{1}{T}\right) + ln(A)$



The smaller the activation energy the great the reaction rate. Therefore, reaction a will have the greatest rate.



The second graph is a two-step problem. 1^{st} : reactants \rightarrow intermediates 2^{nd} : intermediates \rightarrow products. Since the second reaction has the greater activation energy it will be the slower reaction and will determine the rate of the reaction. Therefore, we label the activation energy of the 2^{nd} step.

88.



The activation energy for the reverse reaction is the - ΔE + $E_{a}.$

$$-(-216\frac{kJ}{mol}) + 125\frac{kJ}{mol} = 341\frac{kJ}{mol}$$

- 90. A catalyst increases the reaction rate because it provides another pathway with a lower activation energy for the reaction to proceed by. Homogeneous catalysts are present in the same phase as the reactants and heterogeneous catalyst are present in a different phase from the reactants. The uncatalyzed and catalyzed reactions most likely will have different rate laws because they have different pathways that they occur by.
- 94. a) The catalyst is the species that is initially added to the reaction but not used in the overall reaction. Therefore, NO is the catalyst.
 - b) An intermediate is a species that is formed in one of the steps of the reaction but not one of the reactants or products. Therefore, NO₂ is an intermediate.

c)
$$ln(k) = -\frac{E_a}{R} \left(\frac{1}{T}\right) + ln(A)$$

$$ln(k_{cat}) - ln(k_{uncat}) = -\frac{E_a(cat)}{R} \left(\frac{1}{T}\right) + ln(A) - \left(-\frac{E_a(uncat)}{R} \left(\frac{1}{T}\right) + ln(A)\right)$$

$$ln\left(\frac{k_{cat}}{k_{uncat}}\right) = \frac{1}{RT} \left(-E_a(cat) + E_a(uncat)\right)$$

$$ln\left(\frac{k_{cat}}{k_{uncat}}\right) = \frac{1}{(8.3145 \frac{J}{mol \cdot K})(298 \, K)} \left(-11,900 \, J + 14,000 \, J\right) = 0.848$$

$$\frac{k_{cat}}{k_{uncat}} = 2.3$$